

Answer Key for HW 9

2. [12 pts]

(i) [5 pts] (1 pt for attempt)

$$y(t) = \frac{8}{16 - \omega^2} (\cos \omega t - \cos 4t) = \frac{16}{16 - \omega^2} \sin\left(\frac{\omega + 4}{2}t\right) \sin\left(\frac{4 - \omega}{2}t\right) \quad (\omega \neq 4)$$

[3 pts] [1 pt]

(ii) [2 pts] (1 pt for answer, 1 pt for explanation)

$$\text{Amplitude} = \left| \frac{8}{\omega^2 - 16} \right| \quad \left(\begin{array}{l} \text{'Amplitude is affected by } \frac{8}{\omega^2 - 16} \text{ is also acceptable} \\ (16 - \omega^2 \text{ instead of } \omega^2 - 16 \text{ is also acceptable}) \end{array} \right)$$

(iii) [1 pt] $\omega \rightarrow 4$ ($\omega \rightarrow -4$, $\omega \rightarrow \pm 4$ are also acceptable)

(iv) [1 pt] Decreases ('approaches to 0' is also acceptable)

(v) [3 pts] (.5 pts for attempt) $y(t) = t \sin 4t$

4. [11 pts]

(i) [3 pts] (.5 pts for attempt)

$$y(t) = \frac{1}{37} (e^{3t} + 216e^{-3t} \sin t + 36e^{-3t} \cos t)$$

(ii) [3 pts] (.5 pts for attempt)

$$y(t) = \frac{2}{39} \cos t (e^{-3t} - 1) + \frac{1}{13} \sin t (e^{-3t} + 1) \quad \left(= \left(\frac{\sin t}{13} - \frac{2 \cos t}{39} \right) + e^{-3t} \left(\frac{\sin t}{13} + \frac{2 \cos t}{39} \right) \right)$$

(iii) [3 pts] (.5 pts for attempt)

$$y_p(t) = -\frac{1}{2} e^{-3t} t \cos t$$

(iv) [2 pts] (.5 pts for attempt)

$$y(t) = \frac{e^{3t}}{37} + \frac{t}{10} - \frac{3}{50}$$

7. [7 pts] (1 pt for attempt)

$$y_p(t) = \frac{1}{2} t e^{-3t} \{ \cos t + (t + 1) \sin t \} \quad \left(= \frac{1}{2} e^{-3t} t^2 \sin t + \frac{1}{2} e^{-3t} t \sin t + \frac{1}{2} e^{-3t} t \cos t \right)$$